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A Cell Method Stress Analysis in Thin Floor Tiles Subjected to Temperature Variation

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Abstract The Cell Method is applied in order to model the debonding mechanism in ceramic floor tiles subjected to positive thermal variation. The causes of thermal debonding, very usual in radiant heat floors, have not been fully clarified at the moment. There exist only a few simplified analytical approaches that assimilate this problem to an eccentric tile compression, but these approaches introduce axial forces that, in reality, do not exist. In our work we have abandoned the simplified closed form solution in favor of a numerical solution, which models the interaction between tiles and sub-base more realistically, when the positive thermal variation 12 increases the volume of the sub-base. The thermal problem has been approached as 13 a contact problem in a composite structure. In particular, the kinematic and equilibrium conditions have been imposed at the interface between lower part, which 15 is the sub-base, and the upper part, which is composed by the adhesive, the tiles, 16 and the grouting between the tiles. The failure condition has been studied in the Mohr-Coulomb plane by using the Leon criterion, a unifying criterion that com-18 bines the shear stress with traction and compression. Therefore, we employed a 19 unique failure criterion both for the nodes at the interface between sub-base and 20 adhesive (which undergo a shear/tensile failure or a shear failure) and the nodes 21 at the interface between tiles and grouting (which undergo a tensile failure). This allowed us to model the tile debonding both in the horizontal and in the vertical 23 interfaces, while previous FEM codes treated the tile debonding only on the hori-24 zontal interfaces. The numerical analyses were performed in parametric modality, by varying the geometric and mechanical characteristics of the model. Particular 26 attention was devoted to the modeling of thin tiles, a new type of ceramic tiles, for which there are no yet consensus standards. 28

Keywords: Thin Tiles, Composite Structures, Contact Problem, Failure criteria, Cell Method, Parametric Analysis

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31 1 Introduction

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One of the hottest trends in floor tile market is the emergence of thin tiles. There are three categories of products being marketed as thin tiles. In the first category, tiles are formed using the traditional dust pressing methodology. In the second and third category, tiles are formed using a lamina process, reinforced with fiberglass or polymeric backing materials in the last case. Regardless of category, thin tiles have a much lower breaking strength than regular ceramic tiles. They also are less able to resist impact loading when unsupported.

The main reason for looking at the performance of thin tiles in particular is because of the increasing availability of thin tiles in the floor tile market. This, in turn, is a consequence of a whole range of advantages for manufacturers coming from tiles engineered to be thinner, including carrying out installations over existing floors, eliminating the need for ripping out existing finishing materials in renovation projects, and saving time and money in labor costs.

Made of porcelain, the thin tiles start at thicknesses of about 2.5 mm for walls, going up to about 6 mm for floors, while, until recently, floor tiles were 8 to 12 mm thick. Thin tiles are lightweight, reduce material consumption and require the use of fewer resources to manufacture and ship them.

The question we are trying to answer in this paper is whether or not thin tiles behave better than traditional floor tiles when used on radiant heat floors (Fig.1). In particular, we want to investigate whether using thin tiles would avoid the principal problem of heat radiant floors made from traditional tiles, that of tile separation from the sub-base when the temperature increases (Fig.2).

We treated the radiant heat floor as a composite structure, made up of a lower part, the sub-base, and an upper part, composed of the adhesive, the tiles and the grouting between the tiles (Fig.3). The analysis was performed on the vertical cross section, by using the Cell Method (the CM [Tonti (2001); Ferretti (in press)]), and the failure condition was evaluated both for the adhesive, as in Dong and Atluri (2012), and for the vertical interfaces (between tiles and grouting).

The lower part is the one where the variation in temperature takes place, causing the lower part to change in volume (Fig.4). If the lower part were not bound to the upper part, the change in volume would occur without generating stresses inside the lower part (Fig.4). Actually, the lower part is free to move horizontally over the laying surface, due to the presence of expansion joints at each end of the run of tiles and a thermal insulation layer on the laying surface (Fig.1). This means that the lower part is constrained isostatically and, consequently, the thermal gradient does not induce any stress in it.

When the lower part is bound to the upper part (Fig.5), its constraint degree be-

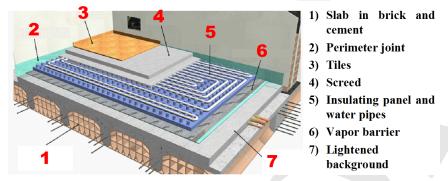


Figure 1: Components of a radiant heat floor



Figure 2: Tile separation from the sub-base in a radiant heat floor [Cocchetti, Comi, and Perego (2011)]

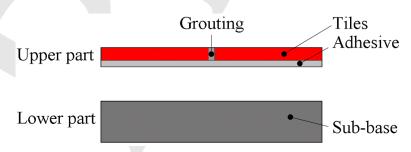
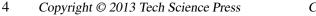


Figure 3: Components of the upper and lower parts in the numerical model



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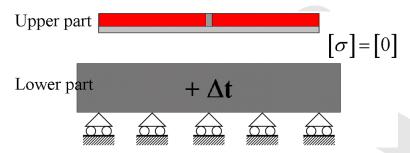


Figure 4: Variation in temperature in the sub-base: isostatic sub-base

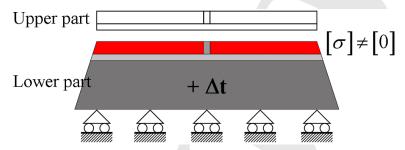


Figure 5: Variation in temperature in the sub-base: hyperstatic sub-base

comes hyperstatic and the interaction between the two parts generates stresses in

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both of them. In the present paper, the interaction between upper and lower parts 70 has been approached as a contact problem, a boundary condition that is easy to treat 71 with the CM, as shown in Ferretti (2013), Ferretti (2004b), and Ferretti (2003a,b), 72 while it is not at all trivial in the differential formulation [Boe, Rodriguez, Plazaola, Banfield, Fong, Caballero, and Vega (2013); Imai and Nakagawa (2012); Blázquez and París (2011); Chen, Cui, Nie, and Li (2011); Yun, Junzhi, Yufeng, and Yiqiang 75 (2011); Hartmann, Weyler, Oliver, Cante, and Hernández (2010); Selvadurai and Atluri (2010); Theilig (2010); Zhou, Li, Yu, and Lee (2010); Chen and Atkinson 77 (2009); Reaz Ahmed and Deb Nath (2009); Willner (2009); Han, Liu, Rajendran, 78 and Atluri (2006)]. The amount of interaction depends on the geometric parameters of the model, 80 specifically the thickness of the adhesive, the thickness of the tiles, the length of 81 the tiles, the number of tiles and the thickness of the grouting. It also depends on the mechanical parameters of the adhesive, the Young modulus and the Poisson 83 modulus. We wish to investigate the effect that each of these parameters have on the 84 separation process. To achieve this, we performed numerical analysis in parametric 85 modality, allowing the operator to define all the parameters. 86

2 Some features of the CM code for crack propagation analysis

Our choice of the CM for the analysis is based on its high degree of detail, which allows us to clarify the mechanisms of stress transfer between the components of the floor. In particular, the CM is capable of capturing corner effects [Ferretti, Casadio, and Di Leo (2008)], providing us with an insight into how stress concentration at the corners of the tiles modifies the principal directions of stress, causing twisting at the corners (Fig. 6). Some examples of how the corner effects are treated in the differential formulation can be found in Zhang (2011), Zheng and Li (2012) and Schnack, Weber, and Zhu (2011).

The picture of the principal directions of stress in Fig.6 was plotted for an increase in temperature in the sub-base, with the length of each segment being proportional to the intensity of the stress at that point. The main principal stresses are those along the horizontal direction, with the sub-base being compressed (blu lines), while the adhesive, the grouting and the tiles are tensioned (red lines). The horizontal compression in the sub-base occurs because the upper part, to which it is bonded, restricts it from expanding freely along the horizontal direction, counteracting the increase in volume of the sub-base that takes place when the temperature increases (Fig.5).

Moreover, we can also see that there is interaction between the tiles and the grouting along the vertical interfaces (Fig.7): the condition of perfect adherence, together with the difference between the two elastic modules, leads to the tiles stretching the grouting along the vertical direction, while the grouting compresses the tiles along the vertical direction. As a consequence, both principal stresses in the grouting are tensile stresses, while the vertical principal stress in the tiles is a compression stress. This phenomenon is clearer in Fig.8, with the colors indicating the sign and the intensity of the vertical normal stresses. Once again, the vertical stress in the tiles is compression stress, while the vertical stress in the grouting is tensile stress.

The deformed configuration in Fig.8 was plotted by amplifying the displacements 100 times. This also makes evident the Poisson effect on the grouting.

The analysis was performed under plane strain conditions and the failure condition was evaluated in the Mohr/Coulomb plane. As is well known, the Mohr criterion (Fig.9) has a bi-linear failure surface, which fits the failure condition in compression well, but it underestimates the ultimate strength for pure shear stress and is unable to calculate the correct direction of propagation both for uniaxial tensile load and pure shear. Since crack propagation in floors takes place, prevalently, due to a combination of traction and shear, the Mohr criterion should be replaced with a criterion that is more restrictive along the axis of uniaxial tensile load. The criterion used here is the Leon criterion [Ferretti (2004a,b); Ferretti (2009)], whose limit sur-

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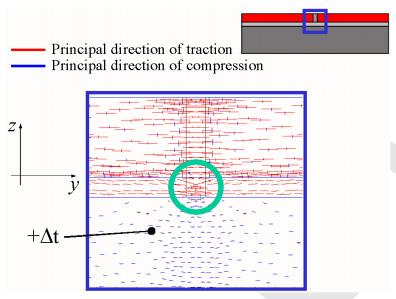


Figure 6: Twisting of the principal directions of stress at the corners of the tiles

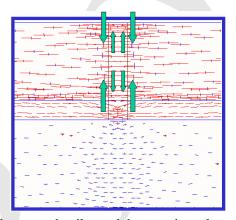


Figure 7: Interaction between the tiles and the grouting, along the vertical interfaces

face has a parabolic shape (Fig.10). The tensile strength for Leon, σ_L , lower than that for Mohr, σ_M , is exactly equal to the tensile strength in uniaxial tensile load, σ_L .

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The analysis in the Mohr/Coulomb plane was performed for the twin nodes of the vertical interfaces between tiles and grouting and for the twin nodes of the laying surface. Each pair of twin nodes provides one point in the Mohr/Coulomb plane,

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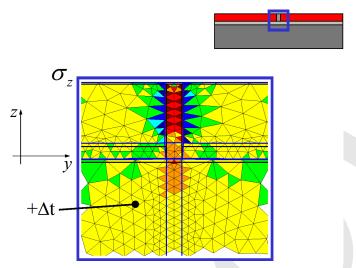


Figure 8: Vertical normal stresses for an increase in temperature in the sub-base

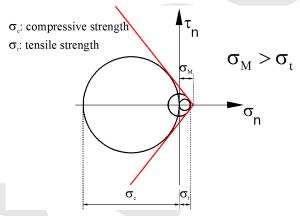


Figure 9: Failure criterion of Mohr and greater circles of Mohr for uniaxial traction, uniaxial compression and pure shear

whose coordinates are the normal and shear stresses in the twin nodes, evaluated over the interface plane.

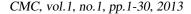
For this particular application, the direction of propagation is known, because the crack propagates along the interface. Thus, in order to identify the direction of propagation, we do not need to build the three circles of Mohr, which give the state of stress at the point, for all the planes passing through the point. Moreover, since the point drawn for the interface plane at the limit condition is the failure point

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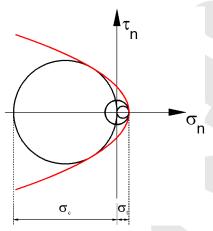


Figure 10: Failure criterion of Leon and greater circles of Mohr for uniaxial traction, uniaxial compression and pure shear

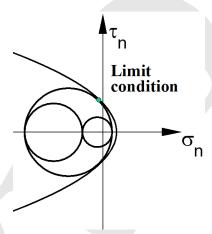


Figure 11: Failure point and circles of Mohr for the twin nodes which are releasing

(Fig.11), we know that, under the assumption of having plotted the circles of Mohr for the limit condition, the greater circle would be tangent to the limit surface of Leon just in the point drawn for the interface plane (Fig.11). With this in mind, evaluating the factor of safety with respect to the propagation is very simple: it is given by d, the distance between the point drawn for the interface plane and the limit surface of Leon (Fig.12), with d greater than zero in safety (Fig.12) and equal to zero when the crack starts propagating (Fig.11).



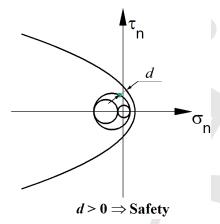


Figure 12: Evaluation of the safety factor in the Mohr/Coulomb plane

3 Numerical results

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Numerical analysis has been performed varying the number of tiles, the elastic modulus of the adhesive, the height of the tiles, the height of the adhesive and the

thickness of the grouting.

The first model we considered is a simplified model made of just two thin tiles,

each with a thickness of 4 mm (Fig.13). Both the adhesive and the grouting are 1

mm thick and the elastic modulus of the adhesive is $8000N/mm^2$.

The stress analysis was performed for an increase in temperature of $30^{\circ}C$ from the

reference temperature, which is the temperature at which the floor was constructed.

Since the first crack enucleates on the vertical interfaces, the ones between tiles

and grouting, we have focused on the twin points of the vertical interfaces, plot-

ting both the stress analysis in the plane of Mohr/Coulomb and the function of the

safety factor (Fig.14), which is the same for both vertical interfaces. In Fig.14, we

have also plotted the normal and shear stresses on the laying surface, between the

adhesive and the sub-base.

For the initial variation in temperature, equal to $1^{\circ}C$, all the points in the Mohr/Coulomb

plane lie inside the failure surface and the factor of safety is greater than zero every-

where along the vertical interfaces (Fig. 14). This means that this temperature does

not induce any cracks along the vertical interfaces and the variation in temperature

164 can be increased.

We can state the same for a variation in temperature of $2^{\circ}C$ (Fig.15): all the points

of the Mohr/Coulomb plane lie inside the limit surface and, consequently, the fac-



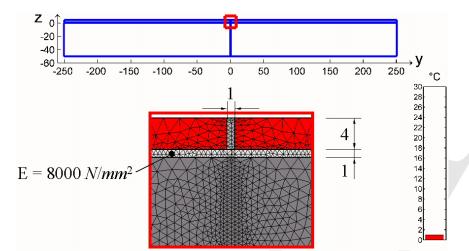


Figure 13: Simplified model, made of two tiles

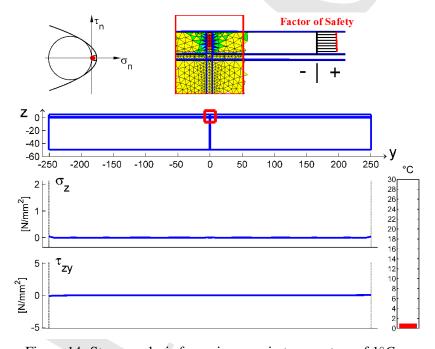


Figure 14: Stress analysis for an increase in temperature of $1^{\circ}C$

tor of safety is greater than zero. Nevertheless, the points of the Mohr/Coulomb plane are nearer to the limit surface, resulting in the factor of safety to decrease

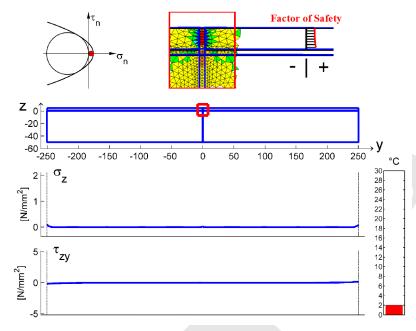


Figure 15: Stress analysis for an increase in temperature of $2^{\circ}C$

everywhere along the vertical interfaces.

At the subsequent increase in temperature (3°*C*), two points of the Mohr/Coulomb plane reach the limit surface, just at the vertex of the parabola (Fig.16). This indicates that a tensile failure condition has been reached on the vertical interfaces. From the plot of the safety factor in Fig.16, we can see that the first points for which the factor of safety is no longer greater than zero are those on the upper corners. Thus, two cracks enucleate on the two upper corners and propagate downwards. The failure of the vertical surfaces enhances the normal stress on the middle point of the horizontal interface under the grouting (Fig.16). This kind of crack propagation is brittle, in the sense that, each time a pair of twin nodes separates, the remaining twin nodes turn out to be more stressed than previously and fail, progressively, for the same value of temperature at which the cracks were enucleated (see Fig.17 for an intermediate step of crack propagation), leading the vertical interfaces to separate completely and the stresses under the grouting to increase further (Fig.18). At the end of the propagation process along the vertical interfaces, the principal directions of stress and the principal stresses turn out to be highly modified (Fig.19).

The new distribution of the stresses can be easily explained in the light of hydrodynamic analogy, taking into account that the two vertical cracks are two obstacles to

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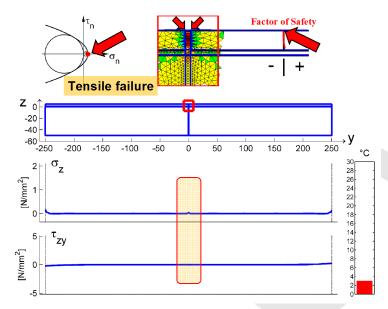


Figure 16: Stress analysis for an increase in temperature of $3^{\circ}C$: first failure condition

the stress flow in the horizontal direction. This is the main cause of the arc effect, well visible in the sub-base.

The greatest difference between the stresses before and after the failure of the vertical interfaces can indeed be observed precisely in the sub-base, where the compression stresses along the horizontal direction have been replaced by tensile stresses arranged in a circle. The presence of traction in this position can explain the radial damage in the sub-base that often appears under the corners together with the separation of the tiles.

By letting the temperature increase further, the next failure condition is reached on the horizontal interface when the factor of safety becomes equal to zero or negative. This takes place at a variation of $7^{\circ}C$ (Fig.20), with a tensile failure at the interface between the grouting and the sub-base. The consequence on the state of stress on the horizontal interface is a knocking down of the peak of the normal stress under the grouting (Fig.21).

This crack propagates at $11^{\circ}C$ for tensile failure (Fig.22) and at $17^{\circ}C$ for a combination of tensile and shear failure (Fig.23).

At $18^{\circ}C$, we have the failure of the end nodes on the horizontal interface (Fig.24), with a knocking down at the ends both for the normal stress and the shear stress

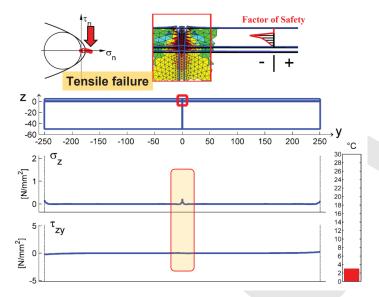


Figure 17: Stress analysis for an increase in temperature of $3^{\circ}C$: intermediate step of crack propagation

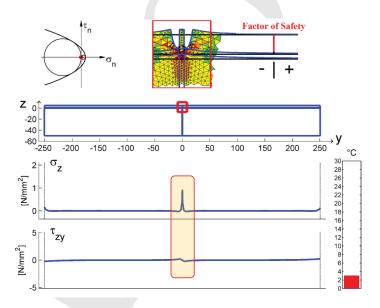


Figure 18: Stress analysis for an increase in temperature of $3^{\circ}C$: end of propagation

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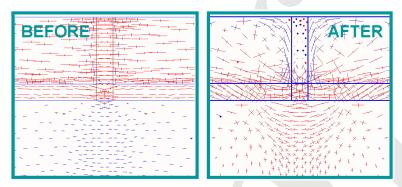


Figure 19: Principal directions of propagation before and after the failure of the vertical interfaces

(Fig.25). The crack under the grouting then extends at $19^{\circ}C$ and $22^{\circ}C$, for a combination of tensile and shear failures in both cases. Finally, at $24^{\circ}C$, the crack on the horizontal interface extends into brittle failure (Fig.26), leading the two tiles to separate from the sub-base almost completely (Fig.28). Consequently, a variation in temperature of $24^{\circ}C$ can be considered as the critical variation in temperature for this simplified model.

During all the propagation process on the horizontal interface, the kind of failure is a shear failure (Fig.27), because the points of the Mohr/Coulomb plane which mostly extrude from the limit surface are those on the shear axis.

At the end of the propagation process, temperature can be increased further, with the separation of a few other pairs of twin nodes on the horizontal interface. The final configuration is shown in Fig.29.

When increasing the number of tiles from 2 to 6, the numerical analysis provides similar results, in the sense that the crack will enucleate on the vertical interfaces also in this case, then under the grouting and, finally, on the ends of the horizontal interface. For each of the five groutings, the vertical cracks propagate downwards along the first of the two interfaces which fail (Fig.30) and upwards, from the adhesive to the upper corner, along the second interface (Fig.31).

The most interesting result is the one concerning the critical variation in temperature, which is $24^{\circ}C$ even when there are 6 tiles (Fig.32).

The analyses performed for 3 and 4 tiles confirmed that the simplified model of just two tiles is able to capture the critical temperature even for models with a greater number of tiles (Fig.32).

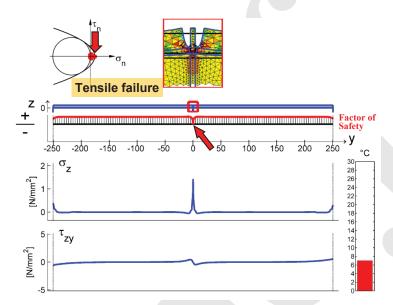


Figure 20: Stress analysis for an increase in temperature of $7^{\circ}C$: failure condition

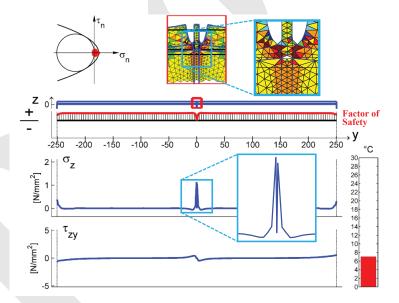


Figure 21: Stress analysis for an increase in temperature of $7^{\circ}C$: domain updating and knocking down of the stress peak



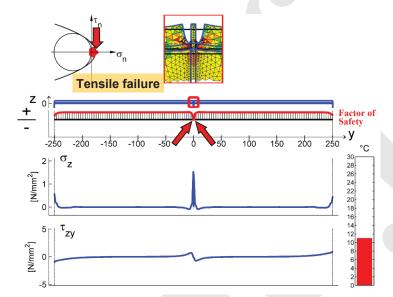


Figure 22: Stress analysis for an increase in temperature of $11^{\circ}C$

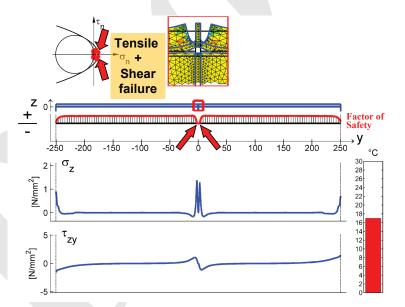


Figure 23: Stress analysis for an increase in temperature of $17^{\circ}C$

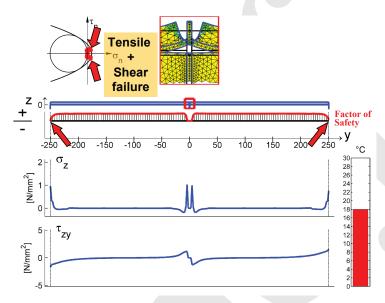


Figure 24: Stress analysis for an increase in temperature of 18°C: failure condition

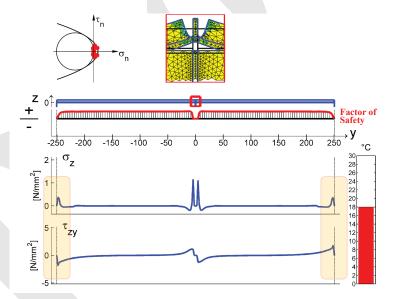
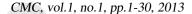


Figure 25: Stress analysis for an increase in temperature of $18^{\circ}C$: domain updating and knocking down of the stress peaks



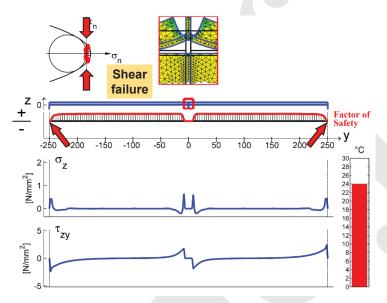


Figure 26: Stress analysis for an increase in temperature of 24°C: first failure condition

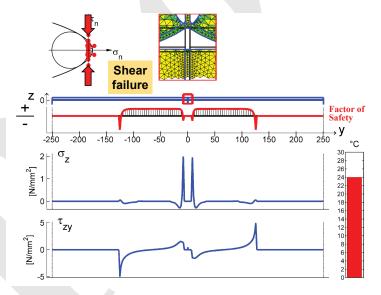


Figure 27: Stress analysis for an increase in temperature of $24^{\circ}C$: intermediate step of crack propagation

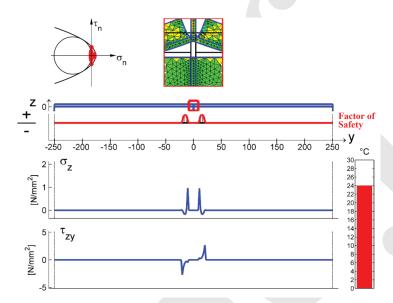


Figure 28: Stress analysis for an increase in temperature of $24^{\circ}C$: final stage of crack propagation

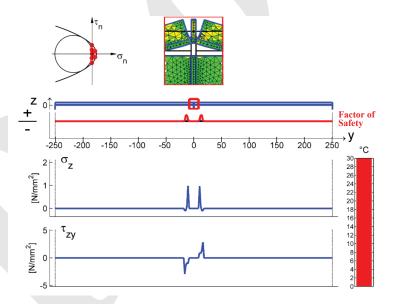
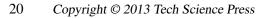


Figure 29: Stress analysis for an increase in temperature of $30^{\circ}C$



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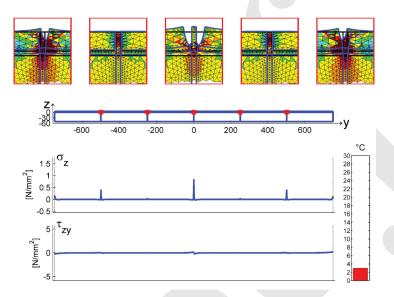


Figure 30: Stress analysis on the model with 6 tiles: downward propagation along the first interface which fails

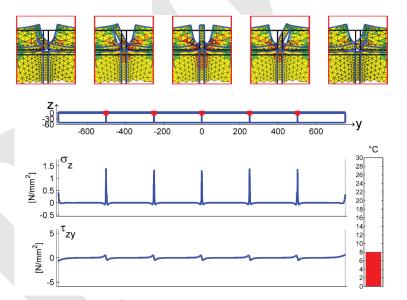


Figure 31: Stress analysis on the model with 6 tiles: upward propagation along the second interface which fails

number of tiles.

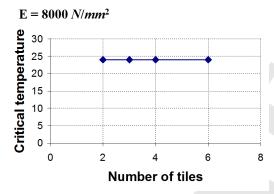


Figure 32: Critical temperature in function of the number of tiles for $E = 8000N/mm^2$

3.1 Parametric analysis on the elastic modulus of the adhesive and the number of tiles

Decreasing the stiffness of the adhesive from 8000 to $3500N/mm^2$ in the simplified model made of 2 tiles, we can notice two different effects on the crack propagation process. The first is the point of enucleation on the vertical interfaces, which is no longer at the upper corners, but at mid-height along the vertical interfaces (Fig.33). The vertical cracks at first propagate upwards and then downwards. The second effect is the critical temperature, which increases from 24 to $29^{\circ}C$ (Fig.34), with a gain of $5^{\circ}C$ (Fig.35). Similarly for the stiffer adhesive, in the model composed of 6 tiles, for each of the five groutings the vertical cracks propagate downwards along the first interface which fails, and upwards, from the adhesive to the upper corner, along the second interface. Moreover, also in this case, increasing the number of tiles does not change the critical temperature, which remains at $29^{\circ}C$ (Fig.36). Since we can

From the analyses on the elastic modulus of the adhesive, we can conclude that less stiff adhesives are preferable to stiffer adhesives, since they increase the critical temperature.

state the same for 3 and 4 tiles (Fig. 37), we may therefore assume that the simpli-

fied models can predict the critical temperature even for the models with a greater

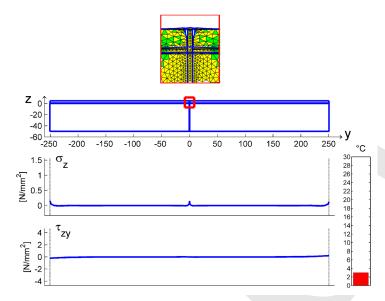


Figure 33: Crack enucleation along the vertical interfaces in the model made of 2 tiles

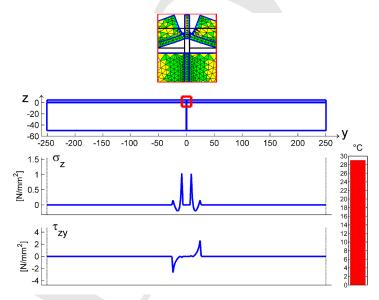


Figure 34: Stress analysis for the critical temperature in the model made of 2 tiles: final stage of crack propagation along the horizontal interface

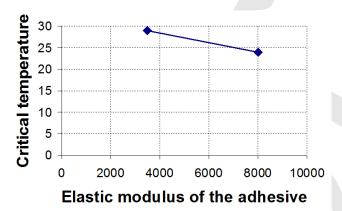


Figure 35: Critical temperature in function of the elastic modulus of the adhesive

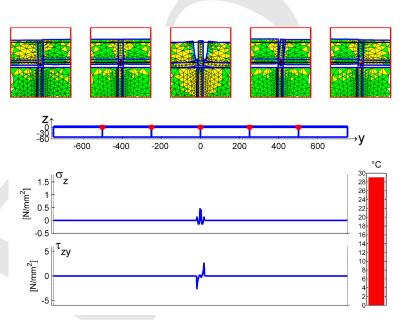


Figure 36: Stress analysis for the critical temperature in the model made of 6 tiles: final stage of crack propagation along the horizontal interface

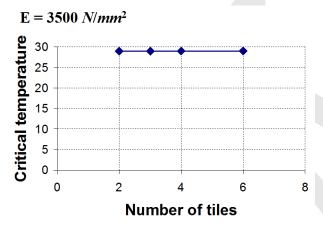


Figure 37: Critical temperature in function of the number of tiles for $E = 3500 N/mm^2$

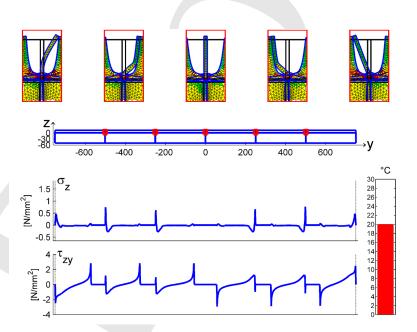


Figure 38: Stress analysis for tiles with a thickness of 12 mm: final stage of crack propagation for an increase in temperature of $20^{\circ}C$

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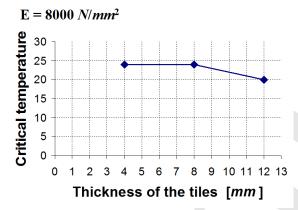


Figure 39: Critical temperature in function of the height of the tiles

In Fig. 38, we have increased the height of the tiles three-fold, obtaining tiles of tra-

3.2 Parametric analysis on the height of the tiles

ditional thickness (equal to 12 mm). The consequence is that the crack propagation on the horizontal interface does not start from the ends, as for the thin tiles, but from the corners of each tile. In particular, the cracks enucleate at the inner corners of the tiles and propagates outwards, toward the center of the tiles (the cracked portions of the horizontal interface in Fig.38 are those where both the normal and shear stresses are equal to 0). This happens for a 20°C variation in temperature, decreasing the critical temperature by $4^{\circ}C$ compared to the model made with the same number of thin tiles (Fig.39). In effect, we can identify two critical temperatures for this model, since the long propagation process activated for $20^{\circ}C$ does not lead, in this model, to the complete separation of the tiles from the sub-base, which occurs at 23°C. The final failure is reached when two cracks enucleate at the ends of the model and propagate inwards. From this analysis, we can conclude that, using tiles of traditional thickness and keeping all the other geometrical and mechanical parameters constant, the horizontal interface under the grouting is more stressed and fails for a temperature lower than the failure temperature for thin tiles. Furthermore, the final critical tempera-

3.3 Parametric analysis on the thickness of the grouting

ture is lower than the failure temperature of the thin tiles.

In terms of the thickness of the grouting, the analyses performed for thicknesses of 1, 2, 3, 4 and 5 mm showed that this does not significantly affect the temper-



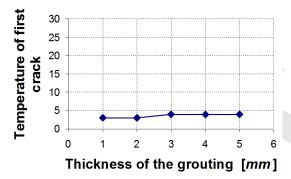


Figure 40: Temperature of first crack in function of the thickness of the grouting

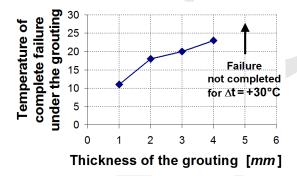


Figure 41: Temperature of complete failure of the grouting in function of its thickness

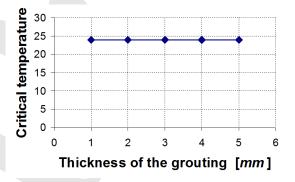


Figure 42: Critical temperature in function of the thickness of the grouting

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ature of first crack along the vertical interface (Fig. 40). The main effect is on the temperature at which the grouting separates from the sub-base, a temperature which increases with the thickness of the grouting (Fig.41). This occurs since the greater thickness of the grouting reduces the stresses over the horizontal interface. Nevertheless, the critical temperature is the same for all the cases: 24°C (Fig.42).

3.4 Parametric analysis on the thickness of the adhesive

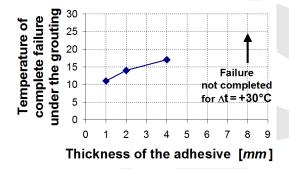


Figure 43: Temperature of complete failure of the grouting in function of the thickness of the adhesive

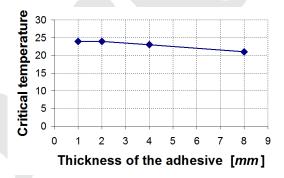


Figure 44: Critical temperature in function of the thickness of the adhesive

Our final analysis was performed on the thickness of the adhesive. We considered thicknesses of 1, 2, 4 and 8 mm. In these cases, the parameter has opposite effects on the failure temperature of the grouting and the critical temperature. The temperature at which the grouting separates from the sub-base increases with the thickness of the adhesive (Fig.43), while the critical temperature progressively decreases when the thickness of the adhesive increases (Fig.44).

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Conclusions 282

- In this paper, it has been proven that the CM can be used to describe the damage 283 effects deriving from the geometrical and elastic parameters of a radiant heat floor, 284 finding that: 285
 - The damaging process of thin tiles is different from the damaging effect of tiles of traditional thickness.
 - Increasing the number of tiles does not change the critical temperature.
- Decreasing the Young modulus of the adhesive increases the critical temper-289 ature. 290
 - Increasing the height of the tiles decreases the critical temperature.
 - Increasing the height of the adhesive decreases the critical temperature.
- Increasing the thickness of the grouting does not change the critical temper-293 ature. 294
- It follows that thin tiles work better than traditional tiles in radiant heat floors, in particular when the adhesive has a low elastic modulus and only a small thickness. 296 We can therefore conclude that radiant heat floors are a very attractive possible field 297 of development and design in the emerging market for thin tiles. 298

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